

# C Interfaces and Implementations

## Quick Reference

Interface summaries are listed below in alphabetical order; the subsections name each interface and its primary type, if it has one. The notation “T is opaque X\_T” indicates that interface X exports an opaque pointer type X\_T, abbreviated as T in the descriptions. The representation for X\_T is given, if the interface reveals its primary type.

The summary for each interface lists, in alphabetical order, the exported variables, excluding exceptions, followed by the exported functions. The prototype for each function is followed by the exceptions it can raise and a concise description. The abbreviations “c.r.e.” and “u.r.e.” stand for checked and unchecked runtime error(s).

The following table summarizes the interfaces by category and gives the pages on which the summaries begin.

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# AP

T is opaque AP\_T

It is a c.r.e. to pass a null T to any AP function.

T AP\_add(T x, T y) Mem\_Failed  
T AP\_addi(T x, long int y) Mem\_Failed  
    return the sum x + y.  
int AP\_cmp(T x, T y)  
int AP\_cmpi(T x, long int y)  
    return an int <0, =0, or >0 if x<y, x=y, or x>y.  
T AP\_div(T x, T y) Mem\_Failed  
T AP\_divi(T x, long int y) Mem\_Failed  
    return the quotient x/y; see Arith\_div. It is a c.r.e. for y=0.  
void AP\_fmt(int code, va\_list \*app, Mem\_Failed  
    int put(int c, void \*cl), void \*cl,  
    unsigned char flags[], int width, int precision)  
    a Fmt conversion function: consumes a T and formats it like printf's %d. It is a c.r.e. for app, \*app, or  
    flags to be null.  
void AP\_free(T \*z)  
    deallocates and clears \*z. It is a c.r.e. for z or \*z to be null.  
T AP\_fromstr(const char \*str, int base, Mem\_Failed  
    char \*\*end)  
    interprets str as an integer in base and returns the resulting T. Ignores leading white space and accepts  
    an optional sign followed by one or more digits in base. For 10<base≤36, lowercase or uppercase letters  
    are interpreted as digits greater than 9. If end≠null, \*end points to the character in str that terminated  
    the scan. If str does not specify an integer in base, AP\_fromstr returns null and sets \*end to str, if  
    end is nonnull. It is c.r.e. for str=null or for base<2 or base>36.

|  |            |
|--|------------|
| T AP_lshift(T x, int s)  | Mem_Failed |
| returns x shifted left by s bits; vacated bits are filled with 0s, and the result has the same sign as x. It is a c.r.e. for s<0.  |            |
| T AP_mod(T x, T y)   | Mem_Failed |
| long AP_modi(T x, long int y)  | Mem_Failed |
| return x mod y; see Arith_mod. It is a c.r.e. for y=0.   |            |
| T AP_mul(T x, T y)   | Mem_Failed |
| T AP_muli(T x, long int y)   | Mem_Failed |
| return the product x·y.  |            |
| T AP_neg(T x)  | Mem_Failed |
| returns -x.  |            |
| T AP_new(long int n)   | Mem_Failed |
| allocates and returns a new T initialized to n.  |            |
| T AP_pow(T x, T y, T p)  | Mem_Failed |
| returns $x^y \bmod p$ . If p=null, returns $x^y$ . It is a c.r.e for y<0 or for a nonnull p<2.                                     |            |
| T AP_rshift(T x, int s)  | Mem_Failed |
| returns x shifted right by s bits; vacated bits are filled with 0s, and the result has the same sign as x. It is a c.r.e. for s<0. |            |
| T AP_sub(T x, T y)   | Mem_Failed |
| T AP_subi(T x, long int y)   | Mem_Failed |
| return the difference x - y.   |            |
| long int AP_toint(T x)   |            |
| returns a long with same sign as x and magnitude $ x  \bmod \text{LONG\_MAX}+1$ .  |            |

```
char *AP_tostr(char *str, int size,  
               int base, T x)
```

Mem\_Failed

fills `str[0..size-1]` with the character representation of `x` in `base` and returns `str`. If `str=null`, `AP_tostr` allocates it. Uppercase letters are used for digits that exceed 9 when `base>10`. It is c.r.e. for a nonnull `str` to be too small or for `base<2` or `base>36`.

# Arena

T is opaque Arena\_T

It is a c.r.e. to pass  $nbytes \leq 0$  or a null T to any Arena function.

```
void *Arena_alloc(T arena, int nbytes, Arena_Failed
    const char *file, int line)
```

allocates *nbytes* bytes in *arena* and returns a pointer to the first byte. The bytes are uninitialized. If `Arena_alloc` raises `Arena_Failed`, *file* and *line* are reported as the offending source coordinate.

```
void *Arena_calloc(T arena, int count, Arena_Failed
    int nbytes, const char *file, int line)
```

allocates space in *arena* for an array of *count* elements, each occupying *nbytes*, and returns a pointer to the first element. It is a c.r.e. for  $count \leq 0$ . The elements are uninitialized. If `Arena_calloc` raises `Arena_Failed`, *file* and *line* are reported as the offending source coordinate.

```
void Arena_dispose(T *ap)
```

deallocates *all* the space in *\*ap*, deallocates the arena itself, and clears *\*ap*. It is a c.r.e. for *ap* or *\*ap* to be null.

```
void Arena_free(T arena)
```

deallocates *all* the space in *arena* — all the space allocated since the last call to `Arena_free`.

```
T Arena_new(void) Arena_NewFailed
```

allocates, initializes, and returns a new arena.

# Arith

`int Arith_ceil(int x, int y)`

returns the least integer not less than the real quotient of  $x/y$ . It is an u.r.e. for  $y \neq 0$ .

`int Arith_div(int x, int y)`

returns  $x/y$ , the maximum integer that does not exceed the real number  $z$  such that  $z \cdot y = x$ . Truncates towards  $-\infty$ ; e.g., `Arith_div(-13, 5)` returns `-3`. It is an u.r.e. for  $y \neq 0$ .

`int Arith_floor(int x, int y)`

returns the greatest integer not exceeding the real quotient of  $x/y$ . It is an u.r.e. for  $y \neq 0$ .

`int Arith_max(int x, int y)`

returns  $\max(x, y)$ .

`int Arith_min(int x, int y)`

returns  $\min(x, y)$ .

`int Arith_mod(int x, int y)`

returns  $x - y \cdot \text{Arith\_div}(x, y)$ ; e.g., `Arith_mod(-13, 5)` returns `2`. It is an u.r.e. for  $y \neq 0$ .

# Array

T is opaque Array\_T

Array indices run from 0 to  $N-1$ , where  $N$  is the length of the array. The empty array has no elements. It is a c.r.e. to pass a null T to any Array function.

T Array\_copy(T array, int length) Mem\_Failed  
creates and returns a new array that holds the initial length elements from array. If length exceeds the length of array, the excess elements are cleared.

void Array\_free(T \*array)  
deallocates and clears \*array. It is a c.r.e. for array or \*array to be null.

void \*Array\_get(T array, int i)  
returns a pointer to the  $i$ th element in array. It is a c.r.e. for  $i < 0$  or  $i \geq N$ , where  $N$  is the length of array.

int Array\_length(T array)  
returns the number of elements in array.

T Array\_new(int length, int size) Mem\_Failed  
allocates, initializes, and returns a new array of length elements each of size bytes. The elements are cleared. It is a c.r.e. for  $length < 0$  or  $size \leq 0$ .

void \*Array\_put(T array, int i, void \*elem)  
copies Array\_size(array) bytes from elem into the  $i$ th element in array and returns elem. It is a c.r.e. for  $elem = \text{null}$  or for  $i < 0$  or  $i \geq N$ , where  $N$  is the length of array.

void Array\_resize(T array, int length) Mem\_Failed  
changes the number of elements in array to length. If length exceeds the original length, the excess elements are cleared. It is a c.r.e. for  $length < 0$ .

int Array\_size(T array)  
returns the size in bytes of the elements in array.

# ArrayRep

T is Array\_T

```
typedef struct T {  
    int length; int size; char *array; } *T;
```

It is an u.r.e. to change the fields in a T.

```
void ArrayRep_init(T array, int length,  
    int size, void *ary)
```

initializes the fields in array to the values of length, size, and ary. It is a c.r.e. for length≠0 and ary=null, length=0 and ary≠null, or size≤0. It is an u.r.e. to initialize a T by other means.



# Assert

`assert(e)`

raises `Assert_Failed` if `e` is 0. Syntactically, `assert(e)` is an expression. If `NDEBUG` is defined when `assert.h` is included, assertions are disabled.

# Atom

It is a c.r.e. to pass a null `str` to any `Atom` function. It is an u.r.e. to modify an atom.

```
int Atom_length(const char *str)
```

returns the length of the atom `str`. It is a c.r.e. for `str` not to be an atom.

```
char *Atom_new(const char *str, int len)
```

Mem\_Failed

returns the atom for `str[0..len-1]`, creating one if necessary. It is a c.r.e. for `len<0`.

```
char *Atom_string(const char *str)
```

Mem\_Failed

returns `Atom_new(str, strlen(str))`.

```
char *Atom_int(long n)
```

Mem\_Failed

returns the atom for the decimal string representation of `n`.

# Bit

T is opaque Bit\_T

The bits in a bit vector are numbered 0 to  $N-1$  where  $N$  is the length of the vector. It is a c.r.e. to pass a null T to any Bit function, except for Bit\_union, Bit\_inter, Bit\_minus, and Bit\_diff.

void Bit\_clear(T set, int lo, int hi)

clears bits lo..hi in set. It is a c.r.e. for lo>hi, or for lo<0 or lo≥N where N is the length of set; likewise for hi.

int Bit\_count(T set)

returns the number of 1s in set.

T Bit\_diff(T s, T t)

Mem\_Failed

returns the symmetric difference  $s \oplus t$ : the exclusive OR of s and t. If s=null or t=null, it denotes the empty set. It is a c.r.e. for s=null and t=null, or for s and t to have different lengths.

int Bit\_eq(T s, T t)

returns 1 if s = t and 0 otherwise. It is a c.r.e. for s and t to have different lengths.

void Bit\_free(T \*set)

deallocates and clears \*set. It is a c.r.e. for set or \*set to be null.

int Bit\_get(T set, int n)

returns bit n. It is a c.r.e. for n<0 or n≥N where N is the length of set.

T Bit\_inter(T s, T t)

Mem\_Failed

returns  $s \cap t$ : the logical AND of s and t. See Bit\_diff for c.r.e.

int Bit\_length(T set)

returns the length of set.

int Bit\_leq(T s, T t)

returns 1 if  $s \subseteq t$  and 0 otherwise. See Bit\_eq for c.r.e.

int Bit\_lt(T s, T t)

returns 1 if  $s \subset t$  and 0 otherwise. See Bit\_eq for c.r.e.

`void Bit_map(T set,`  
    `void apply(int n, int bit, void *cl), void *cl)`  
calls `apply(n, bit, cl)` for each bit in set from 0 to  $N-1$ , where  $N$  is the length of set. Changes to set by `apply` affect subsequent values of bit.

`T Bit_minus(T s, T t)` Mem\_Failed  
returns  $s - t$ : the logical AND of  $s$  and  $\sim t$ . See `Bit_diff` for c.r.e.

`T Bit_new(int length)` Mem\_Failed  
creates and returns a new bit vector of length 0s. It is a c.r.e. for  $length < 0$ .

`void Bit_not(T set, int lo, int hi)`  
complements bits  $lo..hi$  in set. See `Bit_clear` for c.r.e.

`int Bit_put(T set, int n, int bit)`  
sets bit  $n$  to `bit` and returns the previous value of bit  $n$ . It is c.r.e. for  $bit < 0$  or  $bit > 1$ , or for  $n < 0$  or  $n \geq N$  where  $N$  is the length of set.

`void Bit_set(T set, int lo, int hi)`  
sets bits  $lo..hi$  in set. See `Bit_clear` for c.r.e.

`T Bit_union(T s, T t)` Mem\_Failed  
returns  $s \cup t$ : the inclusive OR of  $s$  and  $t$ . See `Bit_diff` for c.r.e.

# Chan

T is opaque Chan\_T

It is a c.r.e. to pass a null T to any Chan function, or to call any Chan function before calling Thread\_init.

T Chan\_new(void) Mem\_Failed

create, initialize, and return a new channel.

int Chan\_receive(T c, void \*ptr, int size) Thread\_Alerted

waits for a corresponding Chan\_send, then copies up to size bytes from the sender to ptr, and returns the number copied. It is a c.r.e. for ptr=null or size<0.

int Chan\_send(T c, const void \*ptr, int size) Thread\_Alerted

waits for a corresponding Chan\_receive, then copies up to size bytes from ptr to the receiver, and returns the number copied. See Chan\_receive for c.r.e.

# Except

T is Except\_T

```
typedef struct T { char *reason; } T;
```

The syntax of TRY statements is as follows;  $S$  and  $e$  denote statements and exceptions. The ELSE clause is optional.

```
TRY S EXCEPT( $e_1$ )  $S_1$  ... EXCEPT( $e_n$ )  $S_n$  ELSE  $S_0$  END_TRY
```

```
TRY S FINALLY  $S_1$  END_TRY
```

```
void Except_raise(const T *e, const char *file, int line)
```

raises exception \*e at source coordinate file and line. It is a c.r.e. for e=null. Uncaught exceptions cause program termination.

```
RAISE(e)
```

raises e.

```
RERAISE
```

reraises the exception that caused execution of a handler.

```
RETURN
```

```
RETURN expression
```

return statement used within TRY statements. It is an u.r.e. to use a C return statement in TRY statements.

```
typedef void (*T)(int code,  
    va_list *app, int put(int c, void *cl), void *cl,  
    unsigned char flags[256], int width, int precision)
```

defines the type of a conversion function, which is called by the Fmt functions when the associated conversion specifier appears in a format string. Here and below, `put(c, cl)` is called to emit each formatted character `c`. Table 14.1 (page 220) summarizes the initial set of conversion specifiers. It is a c.r.e to pass a null `put`, `buf`, `fmt`, or `ap` to any Fmt function, or for a format string to use a conversion specifier that has no associated conversion function.

```
char *Fmt_flags = "-+ 0"
```

points to the flag characters that can appear in conversion specifiers.

```
void Fmt_fmt(int put(int c, void *cl), void *cl,  
    const char *fmt, ...)
```

formats and emits the “...” arguments according to the format string `fmt`.

```
void Fmt_fprint(FILE *stream, const char *fmt, ...)
```

```
void Fmt_print(const char *fmt, ...)
```

format and emit the “...” arguments according to `fmt`; `Fmt_fprint` writes to `stream`, `Fmt_print` writes to `stdout`.

```
void Fmt_putd(const char *str, int len,  
             int put(int c, void *cl), void *cl,  
             unsigned char flags[256], int width, int precision)
```

```
void Fmt_puts(const char *str, int len,  
             int put(int c, void *cl), void *cl,  
             unsigned char flags[256], int width, int precision)
```

format and emit the converted numeric (Fmt\_putd) or string (Fmt\_puts) in `str[0..len-1]` according to Fmt's defaults (see Table 14.1, page 220) and the values of `flags`, `width`, and `precision`. It is a c.r.e. for `str=null`, `len<0`, or `flags=null`.

```
T Fmt_register(int code, T cvt)
```

associates `cvt` with the format character code, and returns the previous conversion function. It is a c.r.e. for `code<0` or `code>255`.

```
int Fmt_sfmt(char *buf, int size,                                     Fmt_Overflow  
            const char *fmt, ...)
```

formats the “...” arguments into `buf[1..size-1]` according to `fmt`, appends a null character, and returns the length of `buf`. It is a c.r.e. for `size≤0`. Raises `Fmt_Overflow` if more than `size-1` characters are emitted.

```
char *Fmt_string(const char *fmt, ...)
```

formats the “...” arguments into a null-terminated string according to `fmt` and returns that string.

```
void Fmt_vfmt(int put(int c, void *cl), void *cl,  
            const char *fmt, va_list ap)
```

See `Fmt_fmt`; takes arguments from the list `ap`.

```
int Fmt_vsfmt(char *buf, int size,                                     Fmt_Overflow  
            const char *fmt, va_list ap)
```

See `Fmt_sfmt`; takes arguments from the list `ap`.



```
char *Fmt_vstring(const char *fmt, va_list ap)
```

See `Fmt_string`; takes arguments from the list `ap`.

# List

T is List\_T

```
typedef struct T *T;
struct T { void *first; T rest; };
```

All List functions accept a null T for any list argument and interpret it as the empty list.

- T List\_append(T list, T tail)  
appends tail to list and returns list. If list=null, List\_append returns tail.
- T List\_copy(T list) Mem\_Failed  
creates and returns a top-level copy of list.
- void List\_free(T \*list)  
deallocates and clears \*list. It is a c.r.e. for list=null.
- int List\_length(T list)  
returns the number of elements in list.
- T List\_list(void \*x, ...) Mem\_Failed  
creates and returns a list whose elements are the “...” arguments up to the first null pointer.
- void List\_map(T list,  
void apply(void \*\*x, void \*cl), void \*cl)  
calls apply(&p->first, cl) for each element p in list. It is an u.r.e. for apply to change list.
- T List\_pop(T list, void \*\*x)  
assigns list->first to \*x, if x is nonnull, deallocates list, and returns list->rest. If list=null, List\_pop returns null and does not change \*x.
- T List\_push(T list, void \*x) Mem\_Failed  
adds a new element holding x onto the front of list and returns the new list.

T List\_reverse(T list)

reverses the elements in list inplace and returns the reversed list.

void \*\*List\_toArray(T list, void \*end)

Mem\_Failed

creates an  $N+1$ -element array of the  $N$  elements in list and returns a pointer to its first element. The  $N$ th element in the array is end.

# Mem

It is c.r.e. to pass `nbytes≤0` to any Mem function or macro.

`ALLOC(nbytes)` Mem\_Failed  
allocates `nbytes` bytes and returns a pointer to the first byte. The bytes are uninitialized.

`CALLOC(count, nbytes)` Mem\_Failed  
allocates space for an array of `count` elements, each occupying `nbytes` bytes and returns a pointer to the first element. It is a c.r.e. for `count≤0`. The elements are uninitialized.

`FREE(ptr)`  
See `Mem_free`.

`void *Mem_alloc(int nbytes, const char *file, int line)` Mem\_Failed  
allocates `nbytes` bytes and returns a pointer to the first byte. The bytes are uninitialized. If `Mem_alloc` raises `Mem_Failed`, `file` and `line` are reported as the offending source coordinate.

`void *Mem_calloc(int count, int nbytes, const char *file, int line)` Mem\_Failed  
allocates space for an array of `count` elements, each occupying `nbytes` and returns a pointer to the first element. It is a c.r.e. for `count≤0`. The elements are uninitialized. If `Mem_calloc` raises `Mem_Failed`, `file` and `line` are reported as the offending source coordinate.

`void Mem_free(void **ptr, const char *file, int line)`  
deallocates `*ptr`, if `*ptr` is nonnull, and clears `*ptr`. It is a c.r.e. for `ptr=null`, and it is an u.r.e. for `*ptr` to be a pointer that was not returned by previous call to a Mem allocation function. Implementations may use `file` and `line` to report memory usage errors.

`void *Mem_resize(void **ptr, int nbytes, Mem_Failed  
const char *file, int line)`  
changes the size of the block at `*ptr` to hold `nbytes` bytes, clears `*ptr`, and returns a pointer to the first byte of the new block. If `nbytes` exceeds the size of the original block, the excess bytes are uninitialized. If `nbytes` is less than the size of the original block, only `nbytes` of its bytes appear in the new block. If `Mem_resize` raises `Mem_Failed`, `file` and `line` are reported as the offending source coordinate. It is a c.r.e. for `ptr=null` or `*ptr=null`, and it is an u.r.e. for `*ptr` to be a pointer that was not returned by a previous call to a `Mem` allocation function.

`NEW(p)` Mem\_Failed  
`NEW0(p)` Mem\_Failed  
allocate a block large enough to hold `*p` and return a pointer to the first byte. `NEW0` clears the bytes, `NEW` leaves them uninitialized.

`RESIZE(ptr, nbytes)` Mem\_Failed  
See `Mem_resize`.

```
typedef unsigned char *T
```

MP functions do  $n$ -bit signed and unsigned arithmetic, where  $n$  is initially 32 and can be changed by `MP_set`. Function names that end in `u` or `ui` do unsigned arithmetic; others do signed arithmetic. MP functions compute their results before raising `MP_Overflow` or `MP_DivideByZero`. It is a c.r.e. to pass a null `T` to any MP function. It is an u.r.e. to pass a `T` that is too small to any MP function.

```
T MP_add(T z, T x, T y)                                MP_Overflow
T MP_addi(T z, T x, long y)                            MP_Overflow
T MP_addu(T z, T x, T y)                                MP_Overflow
T MP_addui(T z, T x, unsigned long y)                  MP_Overflow
    set z to x + y and return z.
T MP_and(T z, T x, T y)
T MP_andi(T z, T x, unsigned long y)
    set z to x AND y and return z.
T MP_ashift(T z, T x, int s)
    sets z to x shifted right by s bits and returns z. Vacated bits are filled with x's sign bit. It is a c.r.e. for s < 0.
int MP_cmp(T x, T y)
int MP_cmpi(T x, long y)
int MP_cmpu(T x, T y)
int MP_cmpui(T x, unsigned long y)
    return an int <0, =0, or >0 if x < y, x = y, or x > y.
```

T MP\_cvt(int m, T z, T x) MP\_Overflow

T MP\_cvtu(int m, T z, T x) MP\_Overflow

narrow or widen x to an m-bit signed or unsigned integer in z and return z. It is a c.r.e. for  $m < 2$ .

T MP\_div(T z, T x, T y) MP\_Overflow, MP\_DivideByZero

T MP\_divi(T z, T x, long y) MP\_Overflow, MP\_DivideByZero

T MP\_divu(T z, T x, T y) MP\_DivideByZero

T MP\_divui(T z, T x, unsigned long y) MP\_Overflow, MP\_DivideByZero

set z to  $x/y$  and return z. The signed functions truncate towards  $-\infty$ ; see Arith\_div.

void MP\_fmt(int code, va\_list \*app, int put(int c, void \*cl), void \*cl, unsigned char flags[], int width, int precision)

void MP\_fmtu(int code, va\_list \*app, int put(int c, void \*cl), void \*cl, unsigned char flags[], int width, int precision)

are Fmt conversion functions. They consume a T and a base  $b$  and format it like printf's %d and %u. It is c.r.e. for the  $b < 2$  or  $b > 36$ , and for app, \*app, or flags to be null.

T MP\_fromint(T z, long v) MP\_Overflow

T MP\_fromintu(T z, unsigned long u) MP\_Overflow

set z to v or u and return z.

T MP\_fromstr(T z, const char \*str, int base, char \*\*end) MP\_Overflow

interprets str as an integer in base, sets z to that integer, and returns z. See AP\_fromstr.

T MP\_lshift(T z, T x, int s)

set z to x shifted left by s bits and return z. Vacated bits are filled with 0s. It is a c.r.e. for  $s < 0$ .

|  |                              |
|--|------------------------------|
| T MP_mod(T z, T x, T y)  | MP_Overflow, MP_DivideByZero |
| sets z to x mod y and returns z. Truncates towards $-\infty$ ; see Arith_mod.    |                              |
| long MP_modi(T x, long y)  | MP_Overflow, MP_DivideByZero |
| returns x mod y. Truncates towards $-\infty$ ; see Arith_mod.                    |                              |
| T MP_modu(T z, T x, T y)   | MP_DivideByZero              |
| sets z to x mod y and returns z.   |                              |
| unsigned long MP_modui(T x, unsigned long y)                                     | MP_Overflow, MP_DivideByZero |
| returns x mod y.   |                              |
| T MP_mul(T z, T x, T y)  | MP_Overflow                  |
| sets z to x·y and returns z.   |                              |
| T MP_mul2(T z, T x, T y)   | MP_Overflow                  |
| T MP_mul2u(T z, T x, T y)  | MP_Overflow                  |
| set z to the <i>double-length</i> result of x·y and return z, which has 2n bits. |                              |
| T MP_muli(T z, T x, long y)  | MP_Overflow                  |
| T MP_mulu(T z, T x, T y)   | MP_Overflow                  |
| T MP_mului(T z, T x, unsigned long y)  | MP_Overflow                  |
| set z to x·y and return z.   |                              |
| T MP_neg(T z, T x)   | MP_Overflow                  |
| sets z to -x and returns z.  |                              |
| T MP_new(unsigned long u)  | Mem_Failed, MP_Overflow      |
| creates and returns a T initialized to u.  |                              |
| T MP_not(T z, T x)   |                              |
| sets z to ~x and returns z.  |                              |



T MP\_or(T z, T x, T y)

T MP\_ori(T z, T x, unsigned long y)  
 set z to x OR y and return z.

T MP\_rshift(T z, T x, int s)  
 sets z to x shifted right by s bits and returns z. Vacated bits are filled with 0s. It is a c.r.e. for s<0.

int MP\_set(int n) Mem\_Failed  
 resets MP to do n-bit arithmetic. It is a c.r.e. for n<2.

T MP\_sub(T z, T x, T y) MP\_Overflow

T MP\_subi(T z, T x, long y) MP\_Overflow

T MP\_subu(T z, T x, T y) MP\_Overflow

T MP\_subui(T z, T x, unsigned long y) MP\_Overflow  
 set z to x - y and return z.

long int MP\_toint(T x) MP\_Overflow

unsigned long MP\_tointu(T x) MP\_Overflow  
 return x as a long int or unsigned long.

char \*MP\_tostr(char \*str, int size, Mem\_Failed  
 int base, T x)  
 fills str[0..size-1] with a null-terminated string representing x in base, and returns str. If str=null, MP\_tostr ignores size and allocates the string. See AP\_tostr.

T MP\_xor(T z, T x, T y)

T MP\_xori(T z, T x, unsigned long y)  
 set z to x XOR y and return z.

# Ring

T is opaque Ring\_T

Ring indices run from 0 to  $N-1$ , where  $N$  is the length of the ring. The empty ring has no elements. Pointers can be added or removed anywhere; rings expand automatically. Rotating a ring changes its origin. It is a c.r.e. to passed a null T to any Ring function.

`void *Ring_add(T ring, int pos, void *x)` Mem\_Failed  
inserts `x` at *position* `pos` in `ring` and returns `x`. Positions identify points between elements; see `Str`. It is a c.r.e. for `pos < -N` or `pos > N+1`, where  $N$  is the length of `ring`.

`void *Ring_addhi(T ring, void *x)` Mem\_Failed  
`void *Ring_addlo(T ring, void *x)` Mem\_Failed  
adds `x` to the high (index  $N-1$ ) or low (index 0) end of `ring` and returns `x`.

`void Ring_free(T *ring)`  
deallocates and clears `*ring`. It is a c.r.e. for `ring` or `*ring` to be null.

`int Ring_length(T ring)`  
returns the number of elements in `ring`.

`void *Ring_get(T ring, int i)`  
returns the `i`th element in `ring`. It is a c.r.e. for `i < 0` or `i ≥ N`, where  $N$  is the length of `ring`.

`T Ring_new(void)` Mem\_Failed  
creates and returns an empty ring.

`void *Ring_put(T ring, int i, void *x)` Mem\_Failed  
changes the `i`th element in `ring` to `x` and returns the previous value. See `Ring_get` for c.r.e.

`void *Ring_remhi(T ring)`  
`void *Ring_remlo(T ring)`  
removes and returns the element at the high end (index  $N-1$ ) or low end (index 0) of `ring`. It is a c.r.e. for `ring` to be empty.

`void *Ring_remove(T ring, int i)`

removes and returns element `i` from `ring`. It is a c.r.e. for  $i < 0$  or  $i \geq N$ , where  $N$  is the length of `ring`.

`T Ring_ring(void *x, ...)`

`Mem_Failed`

creates and returns a ring whose elements are the “...” arguments up to the first null pointer.

`void Ring_rotate(T ring, int n)`

rotates the origin of `ring` `n` elements left ( $n < 0$ ) or right ( $n \geq 0$ ). It is a c.r.e. for  $|n| < 0$  or  $|n| > N$ , where  $N$  is the length of `ring`.

# Sem

T is opaque Sem\_T

```
typedef struct T { int count; void *queue; } T;
```

It is an u.r.e. error to read or write the fields in a T directly, or to pass an uninitialized T to any Sem function. It is a c.r.e. to pass a null T to any Sem function, or to call any Sem function before calling Thread\_init.

The syntax of the LOCK statement is as follows; *S* and *m* denote statements and a T.

```
LOCK(m) S END_LOCK
```

*m* is locked, statements *S* are executed and *m* is unlocked. LOCK can raise Thread\_Alerted.

```
void Sem_init(T *s, int count)
```

sets *s*->count to count. It is an u.r.e. to call Sem\_init more than once on the same T.

```
Sem_T *Sem_new(int count)
```

Mem\_Failed

creates and returns a T with its count field initialized to count.

```
void Sem_wait(T *s)
```

Thread\_Alerted

wait until *s*->count>0, then decrements *s*->count.

```
void Sem_signal(T *s)
```

Thread\_Alerted

increments *s*->count.

# Seq

T is opaque Seq\_T

Sequence indices run from 0 to  $N-1$ , where  $N$  is the length of the sequence. The empty sequence has no elements. Pointers can be added or removed from the low end (index 0) or the high end (index  $N-1$ ); sequences expand automatically. It is a c.r.e. to passed a null T to any Seq function.

void \*Seq\_addhi(T seq, void \*x) Mem\_Failed

void \*Seq\_addlo(T seq, void \*x) Mem\_Failed

adds x to the high or low end of seq and returns x.

void Seq\_free(T \*seq)

deallocates and clears \*seq. It is a c.r.e. for seq or \*seq to be null.

int Seq\_length(T seq)

returns the number of elements in seq.

void \*Seq\_get(T seq, int i)

returns the ith element in seq. It is a c.r.e. for  $i < 0$  or  $i \geq N$ , where  $N$  is the length of seq.

T Seq\_new(int hint) Mem\_Failed

creates and returns an empty sequence. hint is an estimate of the maximum size of the sequence. It is c.r.e for  $hint < 0$ .

void \*Seq\_put(T seq, int i, void \*x)

changes the ith element in seq to x and returns the previous value. See Seq\_get for c.r.e.

void \*Seq\_remhi(T seq)

void \*Seq\_remlo(T seq)

remove and return the element at the high or low end of seq. It is a c.r.e. for seq to be empty.

T Seq\_seq(void \*x, ...) Mem\_Failed

creates and returns a sequence whose elements are the “...” arguments up to the first null pointer.

# Set

T is opaque Set\_T

It is a c.r.e. to pass a null member or T to any Set function, except for Set\_diff, Set\_inter, Set\_minus, and Set\_union, which interpret a null T as the empty set.

T Set\_diff(T s, T t) Mem\_Failed

returns the symmetric difference  $s / t$ : a set whose members appear in only one of s or t. It is a c.r.e. for both  $s=null$  and  $t=null$ , or for nonnull s and t have different cmp and hash functions.

void Set\_free(T \*set)

deallocates and clears \*set. It is a c.r.e. for set or \*set to be null.

T Set\_inter(T s, T t) Mem\_Failed

returns  $s \cap t$ : a set whose members appears in s and t. See Set\_diff for c.r.e.

int Set\_length(T set)

returns the number of elements in set.

void Set\_map(T set,

void apply(const void \*member, void \*cl), void \*cl)

calls apply(member, cl) for each member  $\in$  set. It is a c.r.e. for apply to change set.

int Set\_member(T set, const void \*member)

returns 1 if member  $\in$  set and 0 otherwise.

T Set\_minus(T s, T t) Mem\_Failed

returns the difference  $s - t$ : a set whose members appear in s but not in t. See Set\_diff for c.r.e.

T Set\_new(int hint, Mem\_Failed

int cmp(const void \*x, const void \*y),

unsigned hash(const void \*x))

creates, initializes, and returns an empty set. See Table\_new for an explanation of hint, cmp, and hash.

`void Set_put(T set, const void *member)` Mem\_Failed  
adds member to set, if necessary.

`void *Set_remove(T set, const void *member)`  
removes member from set, if  $\text{member} \in \text{set}$ , and returns the removed member; otherwise, `Set_remove` returns null.

`void **Set_toArray(T set, void *end)` Mem\_Failed  
creates a  $N+1$ -element array that holds the  $N$  members in set in an unspecified order and returns a pointer to the first element. Element  $N$  is end.

`T Set_union(T s, T t)` Mem\_Failed  
returns  $s \cup t$ : a set whose members appear in  $s$  or  $t$ . See `Set_diff` for c.r.e.

# Stack

T is opaque Stack\_T

It is a c.r.e. to pass null T to any Stack function.

int Stack\_empty(T stk)

returns 1 if stk is empty and 0 otherwise.

void Stack\_free(T \*stk)

deallocates and clears \*stk. It is a c.r.e. for stk or \*stk to be null.

T Stack\_new(void)

returns a new, empty T.

Mem\_Failed

void \*Stack\_pop(T stk)

pops and returns the top element on stk. It is a c.r.e. for stk to be empty.

void Stack\_push(T stk, void \*x)

pushes x onto stk.

Mem\_Failed



# Str

The `Str` functions manipulated null-terminated strings. Positions identify points between characters; e.g., the positions in `STRING` are

$$\begin{array}{cccccccc} & 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ -6 & S & -5 & T & -4 & R & -3 & I & -2 & N & -1 & G & 0 \end{array}$$

Two positions can be given in either order. `Str` functions that create strings allocate space for their results. In the descriptions below, `s[i:j]` denotes the substring of `s` between positions `i` and `j`. It is a c.r.e. to pass a nonexistent position or a null character pointer to any `Str` function, except as specified for `Str_catv` and `Str_map`.

```
int Str_any(const char *s, int i, const char *set)
    returns the positive position in s after s[i:i+1] if that character appears in set, or 0 otherwise. It is a
    c.r.e. for set=null.

char *Str_cat(const char *s1, int i1, int j1, Mem_Failed
    const char *s2, int i2, int j2)
    returns s1[i1:j1] concatenated with s2[i2:j2].

char *Str_catv(const char *s, ...) Mem_Failed
    returns a string consisted of the triples in “...” up to a null pointer. Each triple specifies an s[i:j].

int Str_chr(const char *s, int i, int j, int c)
    returns the position in s before the leftmost occurrence of c in s[i:j], or 0 otherwise.

int Str_cmp(const char *s1, int i1, int j1,
    const char *s2, int i2, int j2)
    returns an integer <0, =0, or >0 if s1[i1:j1]<s2[i2:j2], s1[i1:j1]=s2[i2:j2], or
    s1[i1:j1]>s2[i2:j2].
```

`char *Str_dup(const char *s, int i, int j, int n)` Mem\_Failed  
returns `n` copies of `s[i:j]`. It is a c.r.e. for `n<0`.

`int Str_find(const char *s, int i, int j, const char *str)`  
returns the position in `s` before the leftmost occurrence of `str` in `s[i:j]`, or 0 otherwise. It is a c.r.e. for `str=null`.

`void Str_fmt(int code, va_list *app, int put(int c, void *cl), void *cl, unsigned char flags[], int width, int precision)`  
is a `Fmt` conversion function. It consumes 3 arguments: a string and two positions and formats the substring in the style of `printf`'s `%s`. It is a c.r.e. for `app`, `*app`, or `flags` to be null.

`int Str_len(const char *s, int i, int j)`  
returns the length of `s[i:j]`.

`int Str_many(const char *s, int i, int j, const char *set)`  
returns the positive position in `s` after a nonempty run of characters from `set` at the beginning of `s[i:j]`, or 0 otherwise. It is c.r.e. for `set=null`.

`char *Str_map(const char *s, int i, int j, const char *from, const char *to)` Mem\_Failed  
returns the string obtained from mapping the characters in `s[i:j]` according to `from` and `to`. Each character from `s[i:j]` that appears in `from` is mapped to the corresponding character in `to`. Characters that do not appear in `from` map to themselves. If `from=null` and `to=null`, their previous values are used. If `s=null`, `from` and `to` establish a default mapping. It is a c.r.e. for only one of `from` or `to` to be null, for `strlen(from)≠strlen(to)`, for `s`, `from`, and `to` to all be null, or for `from=null` and `to=null` on the first call.

`int Str_match(const char *s, int i, int j, const char *str)`  
returns the positive position in `s` if `s[i:j]` starts with `str`, or 0 otherwise. It is a c.r.e. for `str=null`.

`int Str_pos(const char *s, int i)`  
returns the positive position corresponding to `s[i:i]`; subtracting 1 yields the index of `s[i:i+1]`.

`int Str_rchr(const char *s, int i, int j, int c)`  
is the rightmost variant of `Str_chr`.

`char *Str_reverse(const char *s, int i, int j)` Mem\_Failed  
returns a copy of `s[i:j]` with the characters in the opposite order.

`int Str_rfind(const char *s, int i, int j, const char *str)`  
is the rightmost variant of `Str_find`.

`int Str_rmany(const char *s, int i, int j, const char *set)`  
returns the positive position in `s` before a nonempty run of characters from `set` at the end of `s[i:j]`, or 0 otherwise. It is c.r.e. for `set=null`.

`int Str_rmatch(const char *s, int i, int j, const char *str)`  
returns the positive position in `s` before `str` if `s[i:j]` ends with `str`, or 0 otherwise. It is a c.r.e. for `str=null`.

`int Str_rupto(const char *s, int i, int j, const char *set)`  
is the rightmost variant of `Str_upto`.

`char *Str_sub(const char *s, int i, int j)` Mem\_Failed  
returns `s[i:j]`.

`int Str_upto(const char *s, int i, int j, const char *set)`  
returns the position in `s` before the leftmost occurrence in `s[i:j]` of any character in `set`, or 0 otherwise. It is c.r.e. for `set=null`.

# Table

T is opaque Table\_T

It is a c.r.e. to pass a null T or a null key to any Table function.

```
void Table_free(T *table)
```

deallocates and clears \*table. It is a c.r.e. for table or \*table to be null.

```
void *Table_get(T table, const void *key)
```

returns the value associated with key in table, or null if table does not hold key.

```
int Table_length(T table)
```

returns the number of key-value pairs in table.

```
void Table_map(T table,
```

```
    void apply(const void *key, void **value, void *cl),  
    void *cl)
```

calls apply(key, &value, cl) for each key-value in table in an unspecified order. It is a c.r.e. for apply to change table.

```
T Table_new(int hint,
```

Mem\_Failed

```
    int cmp(const void *x, const void *y),  
    unsigned hash(const void *key))
```

creates, initializes, and returns a new, empty table that can hold an arbitrary number of key-value pairs. hint is an estimate of the number such pairs expected. It is a c.r.e. for hint<0. cmp and hash are functions for comparing and hashing keys. For keys x and y, cmp(x,y) must return an int <0, =0, or >0 if x<y, x=y, or x>y. If cmp(x,y) returns 0, then hash(x) must equal hash(y). If cmp=null or hash=null, Table\_new uses a function suitable for Atom\_T keys.

```
void *Table_put(T table,
```

Mem\_Failed

```
    const void *key, void *value)
```

changes the value associated with key in table to value and returns the previous value, or adds key and value if table does not hold key, and returns null.

`void *Table_remove(T table, const void *key)`

removes the key-value pair from `table` and returns the removed value. If `table` does not hold `key`, `Table_remove` has no effect and returns null.

`void **Table_toArray(T table, void *end)`

`Mem_Failed`

creates a  $2N+1$ -element array that holds the  $N$  key-value pairs in `table` in an unspecified order and returns a pointer to the first element. The keys appear in the even-numbered array elements and the corresponding values appear in the following odd-numbered elements, and element  $2N$  is `end`.

# Text

T is Text\_T

```
typedef struct T { int len; const char *str; } T;
typedef struct Text_save_T *Text_save_T;
```

A T is a descriptor; clients can read the fields of a descriptor, but it is an u.r.e. to write them. Text functions accept and return descriptors *by value*; it is a c.r.e. to pass a descriptor with `str=null` or `len<0` to any Text function.

Text manages the memory for its immutable strings; it is an u.r.e. to write this string space or deallocate it by external means. Strings in string space are not terminated by null characters, because they can contain null characters.

Some Text functions accept positions, which identify points between characters; see Str. In the descriptions below, `s[i:j]` denotes the substring in `s` between positions `i` and `j`.

```
const T Text_cset    = { 256, "\000\001...\376\377" }
const T Text_ascii  = { 128, "\000\001...\176\177" }
const T Text_ucase  = {  26, "ABCDEFGHIJKLMNOPQRSTUVWXYZ" }
const T Text_lcase  = {  26, "abcdefghijklmnopqrstuvwxyz" }
const T Text_digits = {  10, "0123456789" }
const T Text_null   = {   0, "" }
```

are static descriptors initialized as shown.

```
int Text_any(T s, int i, T set)
```

returns the positive position in `s` after `s[i:i+1]` if that character appears in `set`, or 0 otherwise.

```
T Text_box(const char *str, int len)
```

builds and returns a descriptor for the client-allocated string `str` of length `len`. It is a c.r.e. for `str=null` or `len<0`.

T Text\_cat(T s1, T s2) Mem\_Failed  
returns s1 concatenated with s2.

int Text\_chr(T s, int i, int j, int c)  
See Str\_chr.

int Text\_cmp(T s1, T s2)  
returns an int <0, =0, or >0 if s1<s2, s1=s2, or s1>s2.

T Text\_dup(T s, int n) Mem\_Failed  
returns n copies of s. It is a c.r.e. for n<0.

int Text\_find(T s, int i, int j, T str)  
See Str\_find.

void Text\_fmt(int code, va\_list \*app,  
int put(int c, void \*cl), void \*cl,  
unsigned char flags[], int width, int precision)  
is a Fmt conversion function. It consumes a *pointer* to a descriptor and formats the string in the style of printf's %s. It is a c.r.e. for the descriptor pointer, app, \*app, or flags to be null.

char \*Text\_get(char \*str, int size, T s)  
copies s.str[0..str.len-1] to str[0..size-1], appends a null, and returns str. If str=null, Text\_get allocates the space. It is a c.r.e. for str≠null and size<s.len+1.

int Text\_many(T s, int i, int j, T set)  
See Str\_many.

T Text\_map(T s, const T \*from, const T \*to) Mem\_Failed  
returns the string obtained from mapping the characters in s according to from and to; see Str\_map. If from=null and to=null, their previous values are used. It is a c.r.e. for only one of from or to to be null, or for from->len≠to->len.

int Text\_match(T s, int i, int j, T str)  
See Str\_match.

int Text\_pos(T s, int i)

See Str\_pos.

T Text\_put(const char \*str)

Mem\_Failed

copies the null-terminated str into string space and returns its descriptor. It is a c.r.e. for str=null.

int Text\_rchr(T s, int i, int j, int c)

See Str\_rchr.

void Text\_restore(Text\_save\_T \*save)

pops the string space to the point denoted by save. It is a c.r.e. for save=null. It is an u.r.e. to use other Text\_save\_T values that denote locations higher than save after calling Text\_restore.

T Text\_reverse(T s)

Mem\_Failed

returns a copy of s with the characters in the opposite order.

int Text\_rfind(T s, int i, int j, T str)

See Str\_rfind.

int Text\_rmany(T s, int i, int j, T set)

See Str\_rmany.

int Text\_rmatch(T s, int i, int j, T str)

See Str\_rmatch.

int Text\_rupto(T s, int i, int j, T set)

See Str\_rupto.

Text\_save\_T Text\_save(void)

Mem\_Failed

returns an opaque pointer that encodes the current top of the string space.

T Text\_sub(T s, int i, int j)

returns s[i:j].

int Text\_upto(T s, int i, int j, T set)

See Str\_upto.



# Thread

T is opaque Thread\_T

It is a c.r.e. to call any Thread function before calling Thread\_init.

void Thread\_alert(T t)

sets t's alert-pending flag and makes t runnable. The next time t runs, or calls a blocking Thread, Sem, or Chan primitive, it clears its flag and raises Thread\_Alerted. It is a c.r.e. for t=null or to name a nonexistent thread.

void Thread\_exit(int code)

terminates the calling thread and passes code to any threads waiting for the calling thread to terminate. When the last thread calls Thread\_exit, the program terminates with exit(code).

int Thread\_init(int preempt, ...)

initializes the Thread for nonpreemptive (preempt=0) or preemptive (preempt=1) scheduling and returns preempt or 0 if preempt=1 and preemptive scheduling is not supported. Thread\_init may accept additional implementation-defined parameters; the argument list must be terminated with a null. It is c.r.e. to call Thread\_init more than once.

int Thread\_join(T t)

Thread\_Alerted

suspends the calling thread until thread t terminates. When t terminates, Thread\_join returns t's exit code. If t=null, the calling thread waits for all other threads to terminate, and then returns 0. It is a c.r.e. for t to name the calling thread or for more than one thread to pass a null t.

T Thread\_new(int apply(void \*),

Thread\_Failed

void \*args, int nbytes, ...)

creates, initializes, and starts a new thread, and returns its handle. If nbytes=0, the new thread executes Thread\_exit(apply(args)), otherwise, it executes Thread\_exit(apply(p)), where p points to a *copy* of the nbytes block starting at args. The new thread starts with its own, empty exception stack. Thread\_new may accept additional implementation-defined parameters; the argument list must be terminated with a null. It is a c.r.e. for apply=null, or for args=null and nbytes<0.

`void Thread_pause(void)`

relinquishes the processor another thread, perhaps the calling thread.

`T Thread_self(void)`

returns the calling thread's handle.

```
typedef unsigned char *T;
```

An extended-precision unsigned integer is represented in base  $2^8$  by an array of  $n$  digits, least significant digit first. Most XP functions take  $n$  as an argument along with source and destination Ts; it is an u.r.e. for  $n < 1$  or for  $n$  not to be the length of the corresponding Ts. It is an u.r.e. to pass a null T or a T that is too small to any XP function.

```
int XP_add(int n, T z, T x, T y, int carry)
```

sets  $z[0..n-1]$  to  $x + y + \text{carry}$  and returns the carry out of  $z[n-1]$ .  $\text{carry}$  must be 0 or 1.

```
int XP_cmp(int n, T x, T y)
```

returns an int  $<0$ ,  $=0$ , or  $>0$  if  $x < y$ ,  $x = y$ , or  $x > y$ .

```
int XP_diff(int n, T z, T x, int y)
```

sets  $z[0..n-1]$  to  $x - y$ , where  $y$  is a single digit, and returns the borrow into  $z[n-1]$ . It is an u.r.e. for  $y > 2^8$ .

```
int XP_div(int n, T q, T x, int m, T y, T r, T tmp)
```

sets  $q[0..n-1]$  to  $x[0..n-1]/y[0..m-1]$ ,  $r[0..m-1]$  to  $x[0..n-1] \bmod y[0..m-1]$ , and returns 1, if  $y \neq 0$ . If  $y = 0$ ,  $\text{XP\_div}$  returns 0 and leaves  $q$  and  $r$  unchanged.  $\text{tmp}$  must hold at least  $n+m+2$  digits. It is an u.r.e. for  $q$  or  $r$  to be one of  $x$  or  $y$ , for  $q$  and  $r$  to be the same T, or for  $\text{tmp}$  to be too small.

```
unsigned long XP_fromint(int n, T z, unsigned long u)
```

sets  $z[0..n-1]$  to  $u \bmod 2^{8n}$  and returns  $u/2^{8n}$ .

```
int XP_fromstr(int n, T z, const char *str,
               int base, char **end)
```

interprets *str* as an unsigned integer in base using *z*[0..*n*-1] as the initial value in the conversion, and returns the first nonzero carry out of the conversion step. If *end*≠null, \**end* points to the character in *str* that terminated the scan or produced a nonzero carry. See *AP\_fromstr*.

```
int XP_length(int n, T x)
```

returns the length of *x*; that is, the index plus one of the most significant nonzero digit in *x*[0..*n*-1].

```
void XP_lshift(int n, T z, int m, T x, int s, int fill)
```

sets *z*[0..*n*-1] to *x*[0..*m*-1] shifted left by *s* bits, and fills the vacated bits with *fill*, which must be 0 or 1. It is an u.r.e. for *s*<0.

```
int XP_mul(T z, int n, T x, int m, T y)
```

adds *x*[0..*n*-1]·*y*[0..*m*-1] to *z*[0..*n*+*m*-1] and returns the carry out of *z*[*n*+*m*-1]. If *z*=0, *XP\_mul* computes *x*·*y*. It is an u.r.e. for *z* to be the same T as *x* or *y*.

```
int XP_neg(int n, T z, T x, int carry)
```

sets *z*[0..*n*-1] to ~*x* + *carry*, where *carry* is 0 or 1, and returns the carry out of *z*[*n*-1].

```
int XP_product(int n, T z, T x, int y)
```

sets *z*[0..*n*-1] to *x*·*y*, where *y* is a single digit, and returns the carry out of *z*[*n*-1]. It is an u.r.e. for  $y \geq 2^8$ .

```
int XP_quotient(int n, T z, T x, int y)
```

sets *z*[0..*n*-1] to *x*/*y*, where *y* is a single digit, and returns *x* mod *y*. It is an u.r.e. for *y*=0 or  $y \geq 2^8$ .

```
void XP_rshift(int n, T z, int m, T x, int s, int fill)
```

right shift; see *XP\_lshift*. If *n*>*m*, the excess bits are treated as if they were equal to *fill*.

```
int XP_sub(int n, T z, T x, T y, int borrow)
```

sets *z*[0..*n*-1] to *x* - *y* - *borrow* and returns the borrow into *z*[*n*-1]. *borrow* must be 0 or 1.

`int XP_sum(int n, T z, T x, int y)`  
sets  $z[0..n-1]$  to  $x + y$ , where  $y$  is a single digit, and returns the carry out of  $z[n-1]$ . It is an u.r.e. for  $y > 2^8$ .

`unsigned long XP_toint(int n, T x)`  
returns  $x \bmod (\text{ULONG\_MAX} + 1)$ .

`char *XP_tostr(char *str, int size, int base, int n, T x)`  
fills  $str[0..size-1]$  with the character representation of  $x$  in base, sets  $x$  to 0, and returns  $str$ . It is a c.r.e. for  $str = \text{null}$ ,  $size$  to be too small, or for  $base < 2$  or  $base > 36$ .